



STEALING SOME NOTATION FROM BIG O NOTATION TO DEVELOP A NEW MULTITHREADING PRIORITY FORMULA

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ABSTRACT

This work aims to develop the CPU industry by distributing its time between the threads efficiently. To do so, an unprecedentedly developed equation is suggested as a new powerful software to increase the CPU performance. This proposed equation dedicates to solve the problem of children inheriting their parents priorities equivalently without a thoughtful basis in multithreading by involving big O to give threads different values, whose importance is inversely proportional to their $O(n)$ s. The second originality is breaking complexity rule, which considers loop iterations if the threads have the same $O(n)$, since usually threads run on the same computer. Therefore, the ratio (No. of loop's iterations to go/total iterations multiplied by $O(n)$) determines thread importance inversely. The third novelty is replacing Round Robin with Big O and iteration ratio. A parser is applied to seek "for" and "while" tokens for $O(n)$ measuring purposes. Three threads, $p_1 O(n^2)$, $p_2 O(n)$, and $p_3 O(n^2)$, approved the equation with results of 32, 51, and 8 time slices, respectively, during the period 0-1000 ms. Meanwhile, Round Robin gives the children the same slice number.



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I. INTRODUCTION

In modern computer systems, threads are preferred over processes, and multithreading over multitasking [1]. Multithreading has a problem that has not touched before which is the equivalency among the priorities of threads. This problem prevents exploiting the full multithreading utilities efficiently since its objective is to decrease CPU idle time in order to improve system performance, use less memory, and execute context switching in order to share memory and speed up thread switching (scheduling) [2]. The scheduling policy includes these rules: the threads with higher priority receive more CPU time than those with lower priority; a higher priority thread may preempt a lower priority thread; and threads with equal priority receive equal CPU time [3]. The problem is with the third rule because the scheduler gives equal priorities to the children threads without studying their background. For example, any Java program that is executed starts its code from the main function. In order to begin running the code included in the main function, the JVM generates a thread which is referred to as "main thread". The main thread is crucial to understand since it inherits the priority of all other threads, is the source from which they are formed, and must be the last thread to

complete execution at all times as depicted in Figure 1 [4]. Each new process is therefore formed with a single thread that competes using priority over its parent process for the processor with the threads of other processes and shares the private segment and other resources [5].

Therefore, they are given arbitrarily the same priority causing unfair competitive between high and low priorities threads as can be seen in the priority techniques that are used by Java and IBM. So, as known, Java is fully based object-oriented which operates in a multithreading environment where a thread scheduler allocates the processor to a thread based on its priority. Java requires that every thread be given a priority when it is created. Priorities can vary from 1 to 10, with 10 being the highest priority. With IBM, for each thread, the kernel keeps track of a priority value, also known as the scheduling priority. The significance of the thread corresponds in reverse with the priority value, which is a positive integer. In other words, a thread with a lower priority value has higher priority. [6], [7].

Moreover, there are two types of thread priorities: fixed and nonfixed; the fixed-priority has an unchanged value, whereas a nonfixed-priority adjusts depending on the processor-usage penalty, the thread's nice value (20 by default), and the least priority

of user threads (40). A thread's priority value is subject to quick and frequent adjustments. The scheduler's priorities recalculation method is the consequence of the ongoing movement. However, for threads with fixed-priority, this is not the case. Meanwhile, the time slice is the maximum amount of time that a thread can be in charge before it risks being displaced by another thread [8].

There are many efforts has been done to improve the priority or utilize it in other systems. For instant, in [9], Based on the RTCOP framework and using multithreading, an architecture for preemptive layer activation called as PLAM has been presented. The non-exception handling layers can be triggered concurrently using PLAM. More work, the majority of complicated processing issues can be solved by applying the Chip Multiprocessor (CMP) technique, which is known for its good performance and high speed for personal computers and Smartphone [10], [11]. For example, in [12] and [13] Multithreading on Android Matrix multiplication program run on single and multi-core for comparing purposes in order to determine the constraints that stand up as obstacles against accomplishing the best execution of time reduction.

Additionally, multithreading middleware for sensor virtualization is built in both the sensor node and the gateway, which lessens the latency brought on by the virtualization of the sensors. Otherwise, scheduling policy, energy use, and memory resources are the three fundamental networking challenges; [14-16] offer prioritization approach to resolve these problems by spotting in the thread priorities' derivation mechanism that is based on inputs from three different sources: threads, the operating system, and external sources like timers to meet the needs of their unique nature. Else, [17] and [18] demonstrate that, in the best instances, the schedulable utilization for the hardware under consideration is roughly multiplied compared to partitioned scheduling without SMT. On the other hand, time complexity is a crucial component for efficient usage on real platforms to decrease the executing time of the algorithm and the completion time of applications, which results in lowering user waiting time [19].

The size of the input is multiplied by the time complexity of an algorithm to determine how long it will take to run [20]. Time complexity involves in many pieces of research specially these are related to the algorithms. For example, designing algorithms to reduce the schedule time for linear and binary PSO, [21] Develops an algorithm to address the issue of the subsequence matching's inherent time complexity.

Other studies, [22] and [23] identify the most effective Traveling Salesman Problem algorithm by evaluating complexity, which has been confirmed to be polynomial equation. All these works are the most related pieces of research to our paper, and it is noticeable that they are located either in multithreading priority field or time complexity field without combining between them which makes this paper the first attempt. So, in this study, a new priority equation is developed to involve time complexity for deciding the next run thread among threads that have equal priorities. Furthermore, an iteration ratio supports the time complexity taking decision among the same polynomial rank threads.

II. METHODOLOGY

This work suggests a developed Multithreading priority equation to solve the equivalent priorities problem by involving constant $O(1)$ and polynomial $O(n^i)$ times from Big O notation as one of its terms for the first time in the priority world.

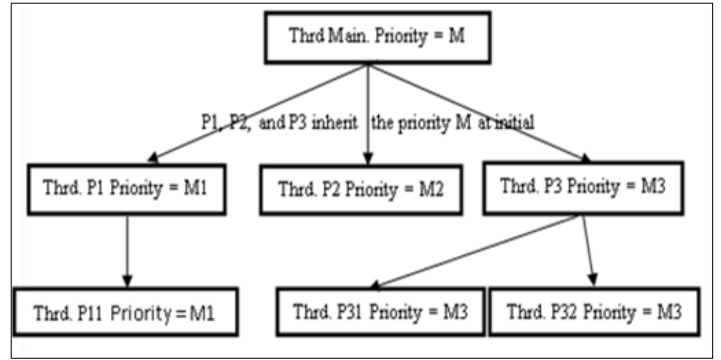


Figure 1: Priority inheriting: P1, P2, and P3 inherit the priority M of the parent Main when they are created. P11 inherits the P1 priority at its creating time $t1 = M1$. P31 and P32 inherit the P3 priority at their creating time $t3 = M3$.

Source: Authors, (2025).

The big O task is the engaging in the equation calculation, Eq. (1), whenever there are equivalent priorities to give them different values which their importance is being inversely with their $O(n^i)$ levels. The second originality is breaking the rule of time complexity which is the number of loop iterations taking part in the equation calculation, Eq. (2), if the threads have the same $O(n^i)$ since usually threads run at the same computer and operating system. Therefore, Eq. (2) is multiplied by $O(n^i)$ to decide thread importance inversely as well. Third novelty is replacing the Round Robin method, which gives the same slice number to all threads with the sane priorities, by Big O and iteration ratio. The time slice is the time that a thread is allowed to consume without interrupting by the scheduler and swapping it with another same priority thread. In this algorithm, the priority value is increased by the CPU usage counter causing lowering the priority since the relation between them is reciprocal. A thread's most recent CPU usage is utilized to determine the processor penalty. At the end of each time slice (10 ms), the recent processor usage value or counter grows by 1, until reaching the value 120 when the swapper recalculates it for all threads. The swapper recalculates the recent processor usage values every second as well. The minimum priority and the nice value in Eq. (1) equal the defaults 40 and 20 respectively [6].

$$Priority = base\ process\ priority + nice\ value + ((time\ slices\ counter) \times (schedo - o\ sched_R)) + (iteration\ ratio \times O(n^i)) \quad (1)$$

$$Iteration\ Ratio = \frac{Number\ of\ loop's\ iterations\ to\ go}{Total\ number\ of\ iterations} \quad (2)$$

Where nice value is the factor that controls the priority and considered a measure of how much the thread cooperates in sharing the CPU, schedo is a CPU scheduler tuning by changing its parameters that are used to calculate threads' priority [6].

For complexity and the iteration ratio part, the formula is applied as is follows:

- 1- The priority of thread = swapper calculation, if its iteration ratio $\times O(n^i)$ is the lowest among all threads.
- 2- If the thread has the lowest (iteration ratio $\times O(n^i)$) among all threads with same $O(n^i)$, then its priority = highest priority among all threads of $O(n^i - 1) + 1$.
- 3- If the thread has higher (iteration ratio $\times O(n^i)$) than other threads which have the same $O(n^i)$, then the thread priority = Highest priority among these threads + 1.

So, instead of giving arbitrary equal priorities for all threads at time zero, time complexity assigns actual priorities at the same time.

II.1 MULTITHREADING

In a multithreading, the priority is assigned to thread by the scheduler of the operating system. There are multi priority levels where each thread is granted a specific priority level according to its importance [24], [25]. With large number of threads and limited resources execution environment, control the priority becomes very crucial to organize threads competing for CPU time [26]. Different operating systems implement different priority scheduling algorithms such as Earliest Deadline First (EDF), Multilevel Feedback Queue Scheduling (MLFQ), and Fixed-Priority Scheduling (FPS). Developing any priority scheduling algorithm always faces two major deficiencies that are thread inversion and starvation. Thread inversion is holding resource by low priority thread when the higher priority thread demands it. Starvation, on the other hand, is depriving a thread with lower priority of CPU time consistently because of overtaking by higher priority threads [27]. Figure 2 illustrates these problems, where threads P1 and P2 share S1 and S2 resources, according to these scenarios: if P1 priority > P2 priority and holds S1 or S2 without releasing and P2 demands that resource, then the starvation occurs. On the other hand, if the same scenario is happened, but with P1 priority < P2 priority, then inversion occurs. These two scenarios are represented by the vertical gray and white box in the figure and vice versa if P2 holds S1 or S2 which may enter P1 into starvation or inversion state represented by the horizontal light gray box in the figure. So, in this work, these two problems are solved by limiting the count of successive time slices that thread may get them. Each algorithm offers advantages and trade-offs, but no one solves the equivalent multithreading priorities, which is unique to this research, by abolition this disorder using a new priority equation, Eq. (1) that has a new pathless concept [28], [29].

II.2 TIME COMPLEXITY

Run time and scalability are the most important parameters to evaluate the algorithms' performances. Since the relation between these features is reversible, algorithms' worst-cases measuring is represented by runtime growth rate verses the increasing of the input size, and big O notation is the tool that is used as measurement for these algorithms which is called a complexity [30], [31]. The complexity of an algorithm is a scale of the data segment that is needed for processing in order to function sufficiently. The number of times the algorithm must execute, relative to the length of the input, is known as time complexity [32], [33]. Since other factors such as operating system, processor power, and programming language are considered, time complexity is not working as a measure of how long a specific algorithm taking to run. Time complexity depicts the run time needed to finish the whole algorithm, not measures exact running time in second or millisecond [34]. So, one of the tools to describe the algorithm time complexity is the Big O notation that applies mathematical equations. These equations include constant time $O(1)$, divide and conquer $O(\log(n))$, polynomials $O(n^i)$, exponentials $O(2^n)$, factorials $O(n!)$ [35]; Table 1 shows some of the runtimes for various algorithms.

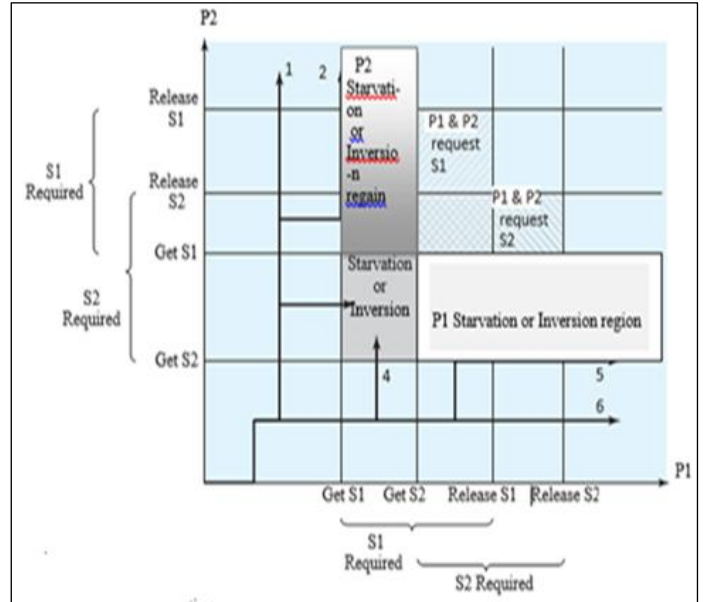


Figure 2: Threads P1 and P2 Starvation and Inversion diagram. P1 execution is represented as x-axis (arrow) and P2 is waiting. P2 execution is represented in the y-axis (arrow) and P1 is waiting.

Source: Authors, (2025).

Where:

- = P1 & P2 request resource S1.
- = P1 & P2 request resource S2.
- = Starvation or Inversion starting region of P1 or P2.
- = Starvation or Inversion region of P1.
- = Starvation or Inversion region of P2.
- = Possible progress path of P and Q.

Horizontal portion of path indicates P is executing and Q is waiting. Vertical portion of path indicates Q is executing and P is waiting.

Since this work is the first work that Big O notation is involving in multithreading priority, just two of its equations, constant and polynomials times, have been chosen to prove the idea since the basic concept is the same for all equations just needed to extend the parser. Figure 3 is the flowchart that illustrates the individual algorithmic loop process to measure the thread complexity that is used in this work by finding nested loop with the highest depth to use it later to specify the thread priority. By tracking the flowchart path, two things are gotten as outputs: first, the highest depth among nested loops, and second, the loop with the largest remaining iteration count. So, from the “into” and “out of” the flowchart the dominant loop is specified which is taking the largest part to the algorithm's runtime. Next, the growth rate of the dominant loop is used in the algorithm's time complexity calculation. So, let's take the bubble sort algorithm as an example to calculate the complexity where the goal of the algorithm is sorting unarranged members. To do so, the number of nested loops is calculated guiding to complexity of $O(n^2)$ because the algorithm needs two loops (nested) to reorder the members [36-38]. A parser

program in C++ has been written to seek “for” and “while” tokens for $O(n^i)$ measuring purposes. The flowchart in Figure 3, depicts the parser flow of the thread algorithm to get its complexity according to the count of nested loops in order to use it in to assign priority to the thread. The second output of the flowchart is the loop with highest remaining iteration count, which is used as priority backup plan to differentiate threads with same complexity.

Table 1:Runtime complexity for various algorithms with least numbers of consecutive operations.

Algorithm	Runtime Complexity	Consecutive Operation
Recurrent	$O(n)$	$O(n)$
Transformer	$O(n^2)$	$O(1)$
Sparse Transformer	$O(n\sqrt{n})$	$O(1)$
Reformer	$O(n\log(n))$	$O(\log(n))$

Source: Authors, (2025).

III. IMPLEMENTATION

For the implementation, this paper applies an experiment with three threads: p1 $O(n^2)$, p2 $O(n)$, and p3 $O(n^2)$ as its steps are shown below where they are started at time $T = 0$ and ended at $T = 1000$ msec. By running the three threads, this information is gotten: p2 needs 70 time slices, meanwhile p1 and p3 need 2817 and 4205 time slices respectively; Figures 4-6 are the screenshots of the number of slices calculation program that are needed by each thread to finish their whole executions. Therefore, p2 should have higher priority and that would not be discovered without time complexity. Furthermore, the iteration ratio supports time complexity by differentiating threads with the same complexity. So, p2 runs first, and then gives up the processor after time slice number 8 because its priority value rises and becomes equivalent to p1 priority values because of CPU usage counter.

Next, iteration ratio gives the control to p1 since iteration numbers of p1 and p2 are 10000000, 15000000 respectively. Here, the iteration ratio is not applied at time zero because it is always equals 1 for all threads. So, the equation assigns at $T = 0$ the priorities 61, 60, 62 to p1, p2, and p3 respectively. Below is the actual calculations based on Eq. (1).

$T = 0$ $p2 = 40 + 20 + (0 * 4/32) = 60$
 p2 takes the control
 $T = 0$ $p1 = p2 + 1 = 61$
 $T = 0$ $p3 = p1 + 1 = 62$
 $T = 10$ ms $p2 = 40 + 20 + (1 * 4/32) = 60$
 $T = 20$ ms $p2 = 40 + 20 + (2 * 4/32) = 60$
 $T = 30$ ms $p2 = 40 + 20 + (3 * 4/32) = 60$
 $T = 40$ ms $p2 = 40 + 20 + (4 * 4/32) = 60$
 $T = 50$ ms $p2 = 40 + 20 + (5 * 4/32) = 60$
 $T = 60$ ms $p2 = 40 + 20 + (6 * 4/32) = 60$
 $T = 70$ ms $p2 = 40 + 20 + (7 * 4/32) = 60$
 $T = 80$ ms $p2 = 40 + 20 + (8 * 4/32) = 61$
 p2 releases control
 $T = 90$ ms $p1 = 40 + 20 + (9 * 4/32) = 61$

 $T = 160$ ms $p1 = 40 + 20 + (16 * 4/32) = 62$
 p1 releases control

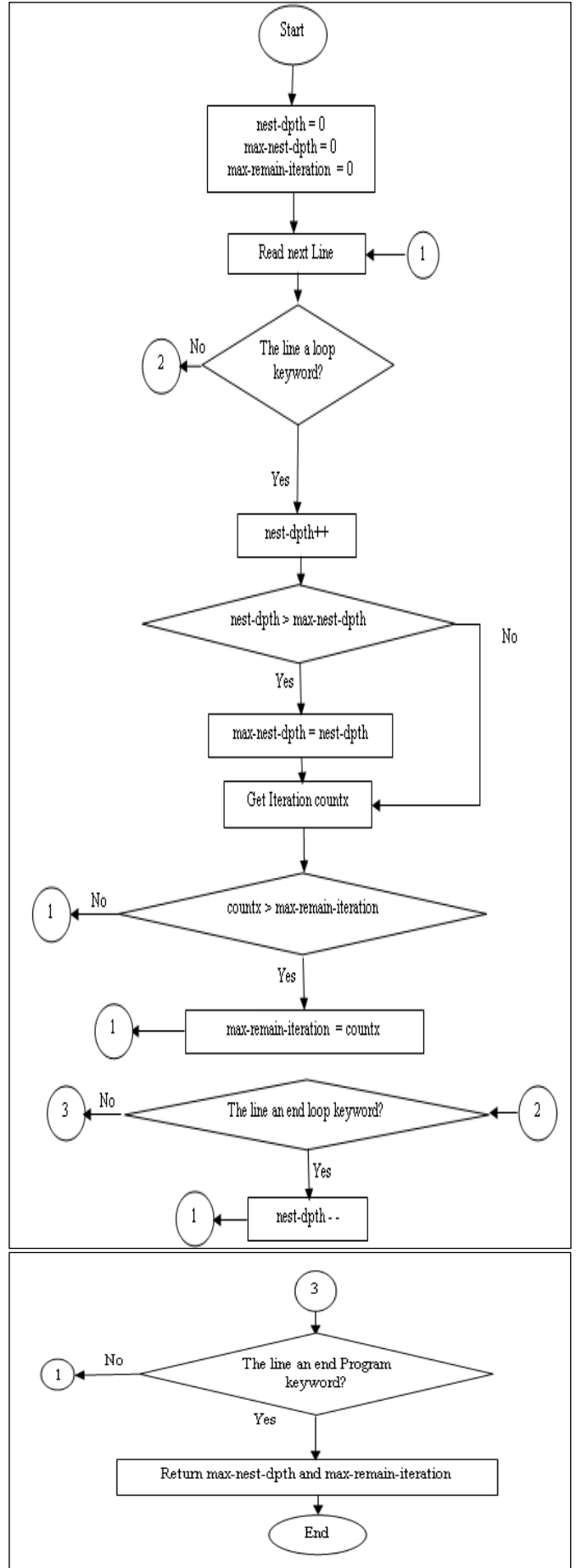


Figure 3: Parser flowchart to get thread complexity according to the count of nested loop with highest depth. Source: Authors, (2025).

Reset counter = 9
 $T = 170\text{ms}$ $p2 = 40 + 20 + (9 * 4/32) = 61$

 $T = 240\text{ms}$ $p2 = 40 + 20 + (16 * 4/32) = 62$
 p2 releases control
 Apply Eq. (1):
 $P1 = 40 + 20 + (17 * 4/32) + ((10000000 - 26418)/10000000 \times 2) = 63.9947164$
 $P2 = 40 + 20 + (17 * 4/32) + ((40000000 - 49835804)/40000000 \times 1) = 62.8754$
 $P3 = 40 + 20 + (17 * 4/32) + (15000000/15000000 \times 2) = 64$

Therefore, $p2 = 62$, $p1 = 63$, $p3 = 64$, so p2 takes control
 $T = 250\text{ms}$ $p2 = 40 + 20 + (17 * 4/32) = 62$

 $T = 320\text{ms}$ $p2 = 40 + 20 + (24 * 4/32) = 63$
 $T = 330\text{ms}$ $p1 = 40 + 20 + (25 * 4/32) = 63$

 $T = 400\text{ms}$ $p1 = 40 + 20 + (32 * 4/32) = 64$
 Reset counter = 25
 $T = 410\text{ms}$ $p2 = 40 + 20 + (25 * 4/32) = 63$

 $T = 480\text{ms}$ $p2 = 40 + 20 + (32 * 4/32) = 64$
 Apply Eq. (1):

$P1 = 40 + 20 + (33 * 4/32) + ((10000000 - 26418)/10000000 \times 2) = 65.9894326$
 $P2 = 40 + 20 + (33 * 4/32) + ((40000000 - 9937962)/40000000 \times 1) = 64.75155095$
 $P3 = 40 + 20 + (33 * 4/32) + (15000000/15000000 \times 2) = 66$
 Therefore, $p1 = 65$, $p2 = 64$, $p3 = 66$, so p2 takes control

$T = 490\text{ms}$ $p2 = 40 + 20 + (33 * 4/32) = 64$

 $T = 560\text{ms}$ $p2 = 40 + 20 + (40 * 4/32) = 65$
 $T = 570\text{ms}$ $p3 = 40 + 20 + (41 * 4/32) = 65$

 $T = 640\text{ms}$ $p3 = 40 + 20 + (48 * 4/32) = 66$

(Skipping forward to 1000msec or 1 second)

$T = 1000\text{ms}$ $p2 = 40 + 20 + (60 * 4/32) = 67$
 $T = 1000\text{ms}$ swapper recalculates the accumulated CPU usage counts of all processes. For the above process:
 $\text{new_CPU_usage} = 67 * 31/32 = 64$ (if $d=31$)
 After decaying by the swapper: $p = 40 + 20 + (64 * 4/32) = 68$
 Apply the equation:
 $P1 = 40 + 20 + (64 * 4/32) + ((10000000 - 26418)/10000000 \times 2) = 69.9788174$
 $P2 = 40 + 20 + (64 * 4/32) + ((40000000 - 15600330)/40000000 \times 1) = 68.6099917$
 $P3 = 40 + 20 + (64 * 4/32) + ((15000000 - 20896)/15000000 \times 2) = 69.997213866$
 Therefore, $p1 = 69$, $p2 = 68$, and $p3 = 70$

Table 2 is a tracing example of p1, p2, and p3, which its explanation is as follows:

At $T = 0$, $p1 = 61$, $p2 = 60$, $p3 = 62$, therefore, p2 controls the CPU since it has the lowest time complexity.

At $T = 90$, p2 relinquishes the control since its priority value becomes equivalent to the p1 priority value = 61. Therefore, p1 takes the control since the iteration ratios for both of p1 and p3 =1,

```
# 93 tick = 307042
# 94 tick = 310261
# 95 tick = 313486
# 96 tick = 316721
# 97 tick = 319967
# 98 tick = 323200
# 99 tick = 326486
# 100 tick = 329601
slicex = 2817

-----
Process exited after 28.59 seconds with return value 0
Press any key to continue . . .
```

Figure 4: P1's total execution slice number calculation. Source: Authors, (2025).

```
# 44 tick = 13437176
# 45 tick = 13740911
# 46 tick = 14059503
# 47 tick = 14386556
# 48 tick = 14652447
# 49 tick = 14963386
# 50 tick = 15281584
# 51 tick = 15600330
# 52 tick = 15912026
# 53 tick = 16217545
# 54 tick = 16534279
# 55 tick = 16852710
# 56 tick = 17165721
# 57 tick = 17481152
# 58 tick = 17796870
# 59 tick = 18112592
# 60 tick = 18429709
# 61 tick = 18746191
# 62 tick = 19059513
# 63 tick = 19368392
# 64 tick = 19671406
# 65 tick = 19991726
# 66 tick = 20309483
# 67 tick = 20620937
# 68 tick = 20929047
# 69 tick = 21237455
# 70 tick = 21541436
slicex = 70

-----
Process exited after 1.277 seconds with return value 0
Press any key to continue . . .
```

Figure 5: P2's total execution slice number calculation. Source: Authors, (2025).

```
# 93 tick = 294699
# 94 tick = 297929
# 95 tick = 301119
# 96 tick = 304329
# 97 tick = 307588
# 98 tick = 310869
# 99 tick = 314147
# 100 tick = 317246
slicex = 4205

-----
Process exited after 42.68 seconds with return value 0
Press any key to continue . . .
```

Figure 6: P3's total execution slice number calculation. Source: Authors, (2025).

Table 2: Tracing of p1, p2, and p3.

T (ms)	p1 Priority	p2 Priority	p3 Priority	CPU control	Counter
0	61	60	62	p2	0
90	61	61	62	p1	1
160	62	61	62	p2	9 reset
240	63	62	64	p2	10
320	63	63	64	p1	11
400	64	63	64	p2	25 reset
480	65	64	66	p2	26
560	65	65	66	p3	27
1000	69	68	70	p2	31

Source: Authors, (2025).

but the number of p1 iterations = 10000000 < 15000000 the number of p3 iterations making p1 = 61 and p3 =62.

At $T = 160$ ms, p1 gives up the control to p2 again since its value rises to 62 while p2 value = 61. But before that, the algorithm reset the counter to 9 the start of value 61 because it reaches 62 while p2 value = 61 which means that p2 will give up the slice right away. For example, the p2 value after one round if the equation applied without resetting the counter is $p2 = 40 + 20 + (17 * 4/32) = 62$ making the algorithm useless.

At $T = 240$ ms, p2 releases the control since its value rises up to 62 and becomes equal to p1 and p3 values. Since all the

threads have equal priorities $p_1 = p_2 = p_3 = 63$, the equation is applied to assign new real priorities. Therefore, the new priorities are $p_1 = 63$, $p_2 = 62$, and $p_3 = 64$. Therefore, p_2 takes the control.

At $T = 320$ ms, $p_2 = 63$ relinquishes the control to $p_1 = 63$ for the second time.

At $T = 400$ ms, $p_1 = 64$ relinquishes the control to $p_2 = 63$ after resetting counter to 25.

At $T = 480$ ms, $p_2 = 64$ relinquishes the control. Since $p_1 = p_2 = p_3 = 64$, the equation is applied and the new priorities are: $p_1 = 65$, $p_2 = 64$, and $p_3 = 66$. p_2 takes the control.

At $T = 560$ ms, $p_2 = 65$ releases control to $p_3 = 66$ in spite of $p_1 < p_3$ since p_1 has the control two consecutive times.

At $T = 1000$ ms (1 sec), swapper recalculates the accumulated CPU usage counter, when thr_1 , thr_2 , and thr_3 had 32, 51, and 8 time slices respectively and the number of completed iterations for each thread are 26418, 15600330, and 20896 respectively. Therefore, $p_1 = 69$, $p_2 = 68$, and $p_3 = 70$, so p_2 takes the control.

From the trace, it is clear that the goal is accomplished since p_2 has 51 slices, p_1 has 32 slices, and p_3 has 8 slices during the period of time 0-1000 ms. Meanwhile, traditional method, which applies Round Robin, gives the same opportunity to the all threads with the same priorities. The concept of this experiment is giving thread with lowest time complexity and loop iterations more time slices. Therefore, they are involving in the equation whenever the priorities of all threads become equivalent because this state turns the equation to Round Robin and gives equal time slices for every thread. So, the task is giving different priorities for each thread whenever this state occurs. Completing the concept, any state rather than the above one, the time complexity will not involve in the priority calculation, but instead Round Robin is replaced with it. So, every time there are two or more threads with the same priority but not all threads, the time complexity and iteration ratio decide the next thread to control the CPU instead of FIFO, which is used by Round Robin method. To avoid starvation among threads with the same time complexity, the algorithm takes the control from the thread with lower iteration ratio and gives it to the other threads after every two consecutive turns. For example, in this work, thr_1 iteration number = 10000000, while thr_3 iteration number = 15000000, so thr_1 is always taking the control since its iteration number to go is always decreasing, meanwhile thr_3 time to go iteration number stays still 15000000.

IV. CONCLUSION

- 1- This work represents a new generation where is no concept of multithreading with equivalent priorities.
- 2- The technique acts as Round Robin with multithreading that have constant time for all threads since there is no loops to calculate their iteration ratios
- 3- This equation rules out the first in first out approach including Round Robin from multithreading system.
- 4- This work does not work with threads having time complexity involving log, exponential, and factorial times, but extending the parser to include them solve it.
- 5- The starvation avoidance can be manipulated by changing the number of consecutive call times.
- 6- The probability that the next time slice is allocated to a thread which has allocated many time slices recently is decreasing.
- 7- Since time complexity considers the time of iterations' numbers trivia, the equation works more efficient with single-processor than multi-processor.

V. AUTHOR'S CONTRIBUTION

Conceptualization: Abdulmir Abdullah Karim, Yaser Ali Enaya and Ghassan Abdulhussein Bilal.

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Discussion of results: Abdulmir Abdullah Karim, Yaser Ali Enaya and Ghassan Abdulhussein Bilal.

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Resources: Yaser Ali Enaya and Ghassan Abdulhussein Bilal.

Supervision: Yaser Ali Enaya and Ghassan Abdulhussein Bilal.

Approval of the final text: Abdulmir Abdullah Karim, Yaser Ali Enaya and Ghassan Abdulhussein Bilal.

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